

# Non-linear radiative response to patterned global warming due to convection aggregation

Heng Quan ([hengquan@princeton.edu](mailto:hengquan@princeton.edu))

Bosong Zhang, Chenggong Wang, Stephan Fueglistaler

## Motivation

The **Green's Function (GF)** approach promises insights into the **pattern effect** using the linear sum of the responses to localized SST perturbations

$$\Delta\bar{R} = \sum_x \frac{\partial\bar{R}}{\partial\text{SST}(x)} \cdot \Delta\text{SST}(x)$$

to predict the change in top of atmosphere radiative fluxes (R) for an arbitrary geographical pattern of SST changes. Question:

Is the **additivity** condition satisfied?

## Conclusions

The GF approach **fails** for **large** SST warming perturbations (i.e. **future global warming**) due to the **non-additivity** of **convection aggregation responses**.

**Convection aggregation** is also responsible for the **outsized response** to **patterned** global warming. Accurate estimation of **climate sensitivity** requires accurate estimation of **convection aggregation**, which is **beyond the scope of linear methods like GF**.

## Non-additivity of the TOA radiative flux responses

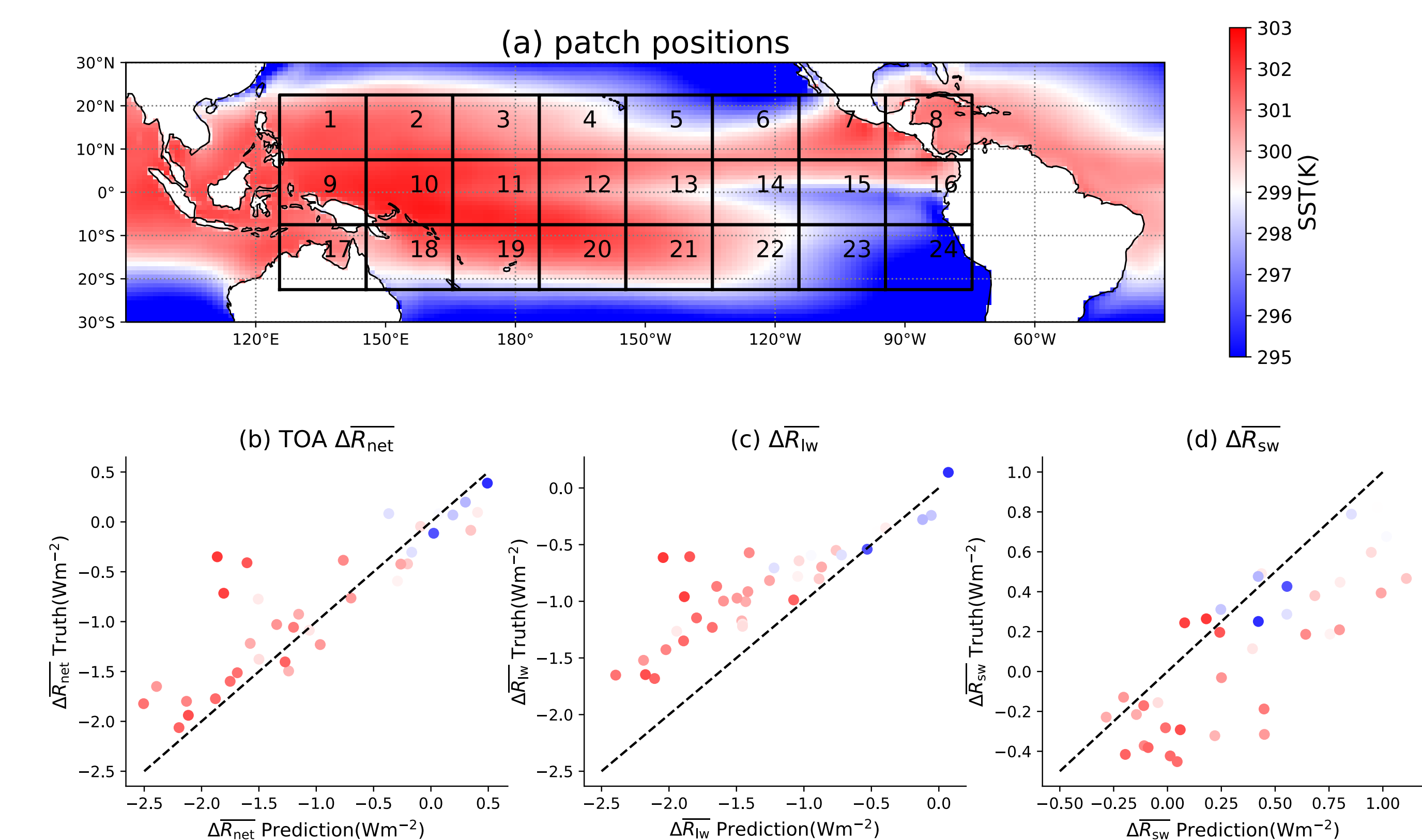


Fig.1: (a) Climatological annual mean SST of base simulation, and grid for SST perturbations. (b) – (d) Green's function prediction (x-axis) and model result (y-axis) for the warming of two adjacent patches of total, longwave and shortwave TOA flux perturbation.

Simulations with GFDL's AM4 atmospheric GCM show (SST+4K):

- (i) SST warming in **warm patches** has **stronger** radiation response.
- (ii) Two adjacent patches SST + 4K, **linear superposition** (prediction by the GF approach) **overestimates** the true response. Warmer patches have larger errors.
- (iii) Partial **cancellation of errors** between  $\Delta\bar{R}_{lw}$  and  $\Delta\bar{R}_{sw}$ .

## The role of large-scale convection aggregation

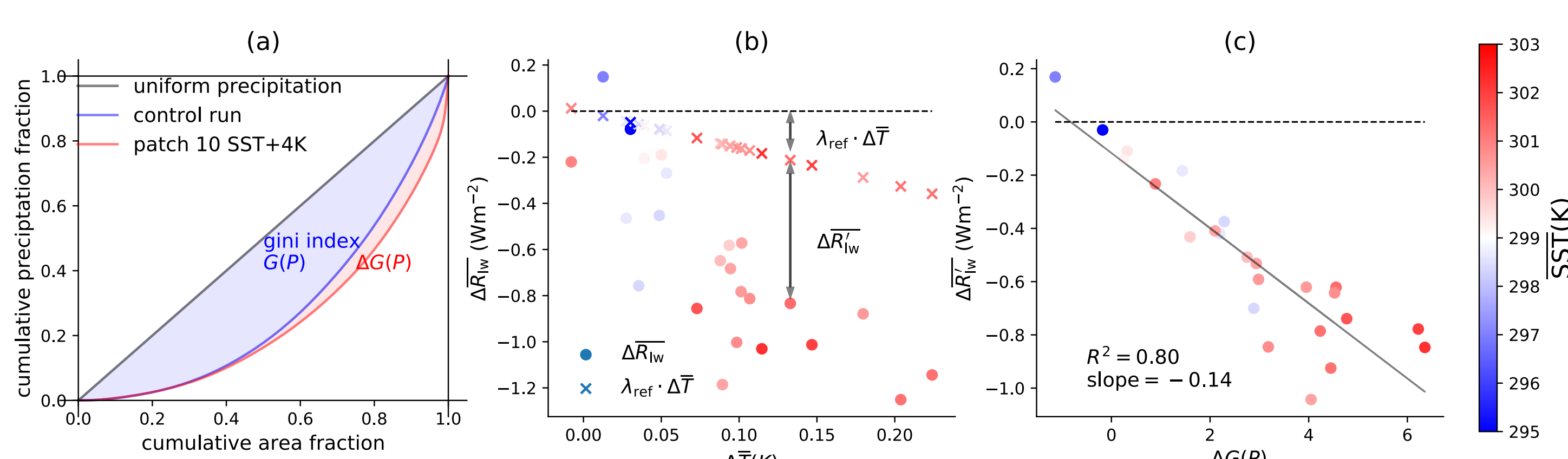


Fig.2 (a) Schematic of tropical rainfall Gini index  $G(P)$ . (b) Longwave radiation response to single patch SST + 4K perturbation, decomposed as  $\Delta\bar{R}_{lw} = \lambda_{ref} \cdot \Delta\bar{T} + \Delta\bar{R}_{lw}'$ , where  $\lambda_{ref} = -1.6\text{Wm}^{-2}$  is the longwave feedback in  $4 \times \text{CO}_2$  simulation, and  $\Delta\bar{R}_{lw}'$  is the "pattern effect". (c)  $\Delta\bar{R}_{lw}'$  is linearly related to Gini index change  $\Delta G(P)$  representing convection aggregation response.

The **Gini index** of tropical rainfall  $G(P)$  measures the **spatial unevenness** of rainfall and **convection aggregation** strength. We find:

$$\Delta\bar{R}_{lw}' \propto \Delta G(P)$$

Longwave radiation response to single patch SST + 4K perturbation  $\Delta\bar{R}_{lw}$  is dominated by  $\Delta\bar{R}_{lw}'$  (departure from  $4 \times \text{CO}_2$  scenario):

$$\Delta\bar{R}_{lw} = \lambda_{ref} \cdot \Delta\bar{T} + \Delta\bar{R}_{lw}'$$

$\Delta\bar{R}_{lw}'$  is caused by convection aggregation response (mid tropospheric drying and high cloud reduction).

## Non-additivity of convection aggregation responses

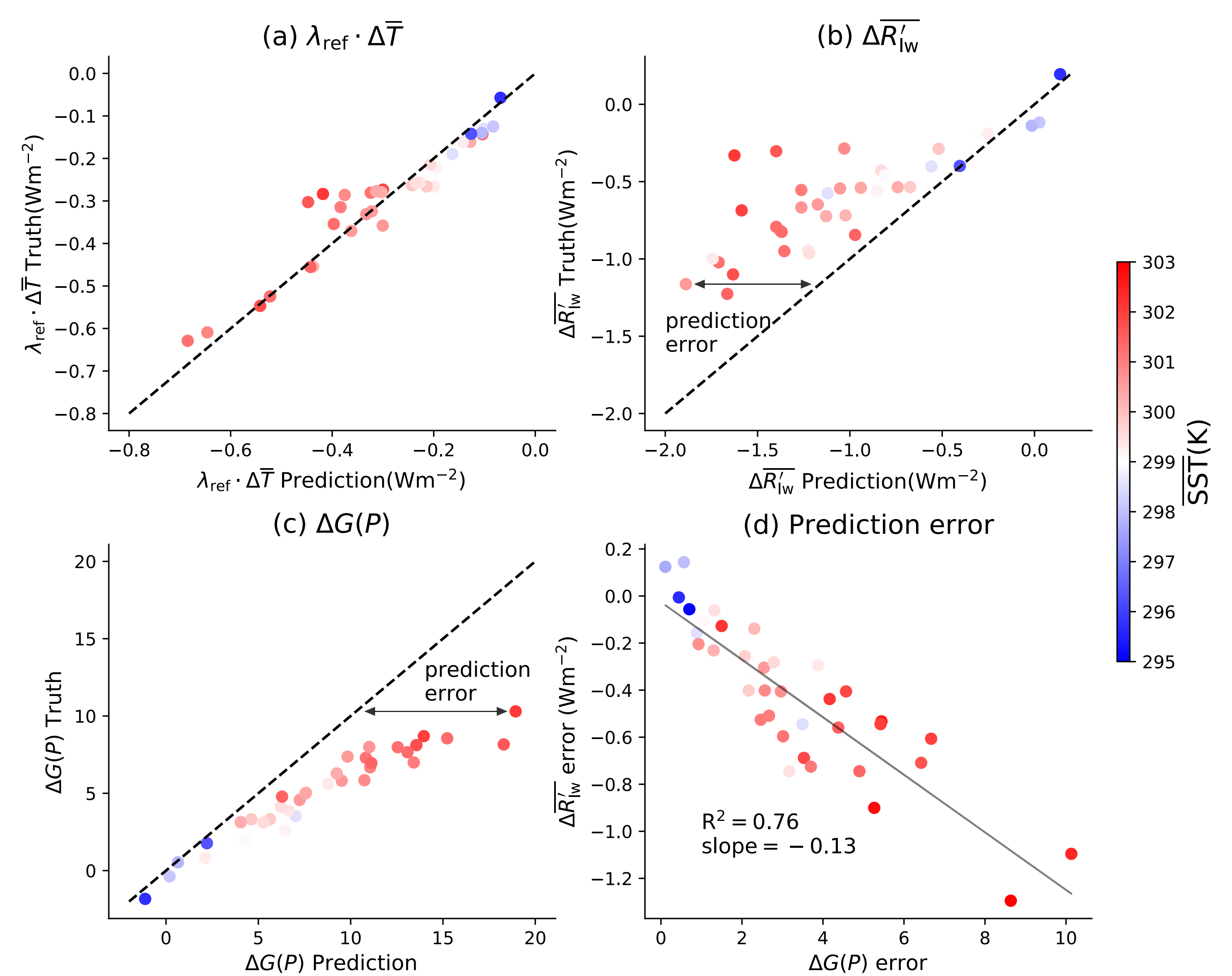


Fig.3 Prediction v.s. truth for (a)  $\lambda_{ref} \cdot \Delta\bar{T}$ ; (b)  $\Delta\bar{R}_{lw}'$  and (c)  $\Delta G(P)$ . (d) The prediction error of  $\Delta\bar{R}_{lw}'$  as function of precipitation Gini index change  $\Delta G(P)$ .

The GF approach **prediction error** in  $\Delta\bar{R}_{lw}$  is dominated by error in  $\Delta\bar{R}_{lw}'$ , which is caused by **prediction error in convective aggregation  $\Delta G(P)$** .

## Dependence of non-additivity on patch size

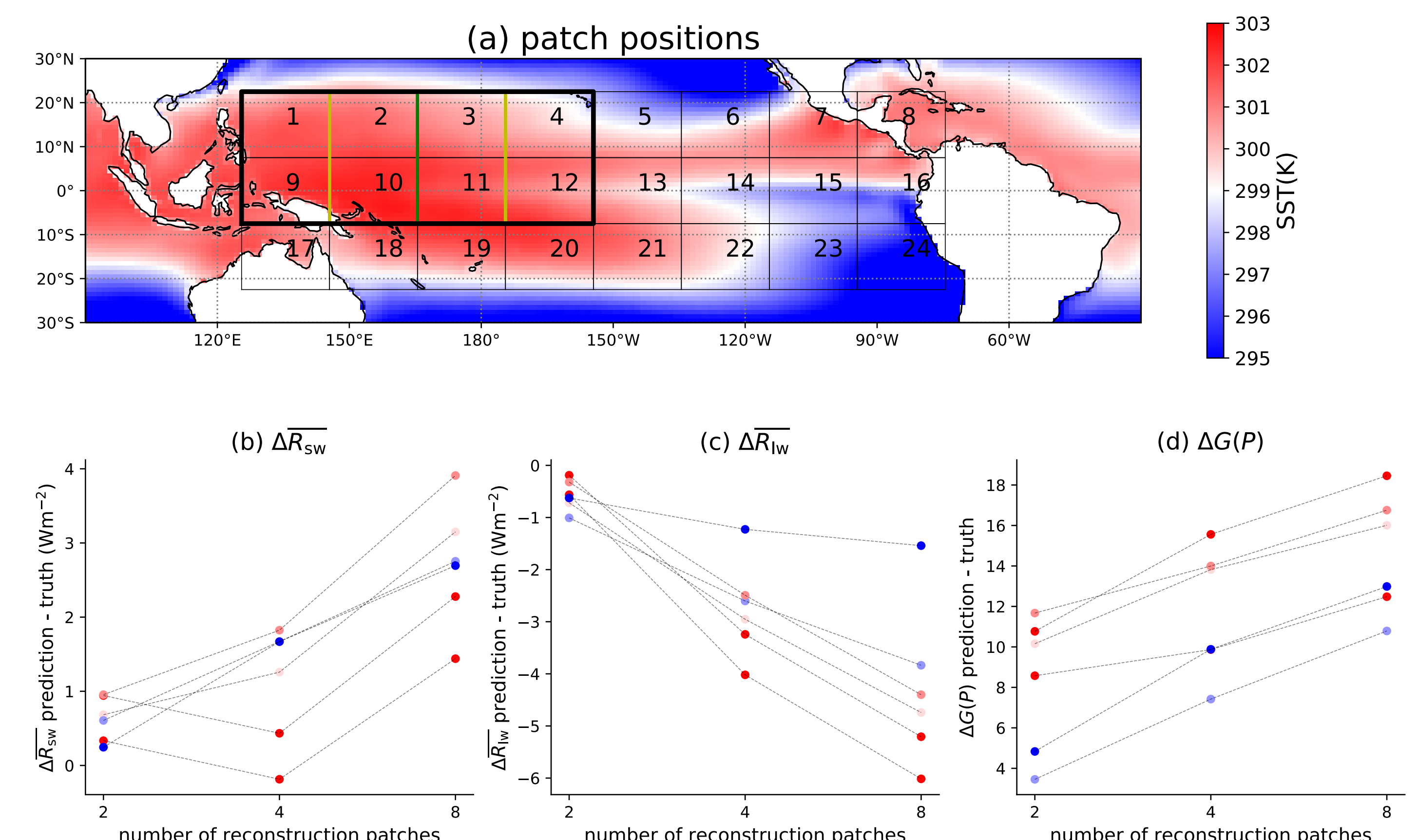


Fig.3 GF prediction of changes following an SST perturbation in an 8-patch area (a), based on linear sum of responses to 8 single patch, 4 two-patch, and 2 four-patch responses; for (b) shortwave and (c) longwave radiation, and (d) the precipitation Gini index.

The GF approach error is **larger** for **smaller** (or equivalently, **more**) patches. **The GF approach is not valid**.